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Книга доктора Даниэля Каплана и профессора Леона Гласса «Понимание нелинейной динамики» рассчитана на студентов выпускных курсов университетов по специальностям: биология, биохимия и биофизика. Книга в доступной форме служит введением в современные проблемы нелинейной динамики. Она содержит главы об устойчивости, мультистабильности, клеточных автоматах и активных средах, фракталах, размерности, циклах и хаосе. В отдельную главу вынесен материал по численному анализу временных рядов, являющийся важным для экспериментальных исследований динамики нелинейных систем.

Книга не претендует на строгое математическое описание рассматриваемых проблем, предполагая, что студенты имеют соответствующую подготовку по физико-математическим дисциплинам университетских программ. В то же время книга содержит большое количество интересных примеров и задач прикладного характера, что очень важно для стимулирования самостоятельной работы.

Книга написана интересно, доступным языком и будет полезна в качестве учебного пособия по прикладной нелинейной динамике студентам, изучающим науки о жизни.

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UNDERSTANDING NONLINEAR DYNAMICS

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